

PhD thesis proposal

## Verifying timed cybersecurity properties in the presence of energy constraints

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## Context

The pervasiveness of cyber-physical systems is highly increasing, raising many safety and security concerns. For instance, the observation of a user's interactions with a system should not give secret information to an attacker. Take the example of an attacker trying to guess a password by writing down a random input. If the system follows a naive algorithm to check the correctness of the password (i.e., checking if every letter is correct one by one and returning "false" as soon as a wrong letter is detected), the attacker can guess how many of the first letters of their input are correct. In order to deal with this kind of issue, we request systems to be *opaque*, meaning that secret behaviors of the system (the correct password) give the same observations to an attacker as some public behaviors of the system. These observations may include timing delays, energy consumption, etc.

Formal methods aim at tackling problems such as opacity through the verification of formal properties on a model abstracting the real system. A well-known formal model to reason about timed systems is *timed automata* [AD94], an extension of finite-state automata with continuous clocks measuring time. Timed automata have been extensively used to verify safety properties, but not so much security properties, with some exceptions (e.g., [Cas09; Ben+15; WZ18; WZA18; Amm+21; And+22; KSA22; ALM23; ADL24]).

## Subject

The objective of the thesis will be to study opacity properties for timed automata, with a strong focus on timing information as was done in [And+22]; in addition, the presence of energy constraints will be interesting, to model energy consumption, or costs [Beh+01; Lar+01; ALP04; Bri+22]. That is, the main challenge will be to study the decidability of the following problem: given a system modeled by a priced/cost/energy timed automaton, can the attacker deduce private information by only looking at the execution time and/or the energy consumption?

Different directions will be envisioned during the thesis:

1. Decidability: studying decidability of various notions of opacity with respect to energy.
2. Expiring opacity: studying decidability of *expiring* opacity [Amm+21; ALM23], i.e., when the secret has an expiration date.
3. Parametric verification: parameters (encoding either timing uncertainty or energy uncertainty [AHV93; Bac+21]) can be used in the model to represent a partial knowledge of the real system or some freedom of choice one has during its design. We are then interested in identifying for which values of the parameters the system is opaque.
4. Depending on the findings, the algorithms developed during the thesis might be implemented in some open-source software, in order to be validated against benchmarks. A typical software candidate is of course IMITATOR, developed by Étienne André and Laure Petrucci [And21; NPP18].

## Keywords

Formal methods, cybersecurity, opacity, energy

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